

The *Stable Paths Problem* As A Model Of BGP Routing

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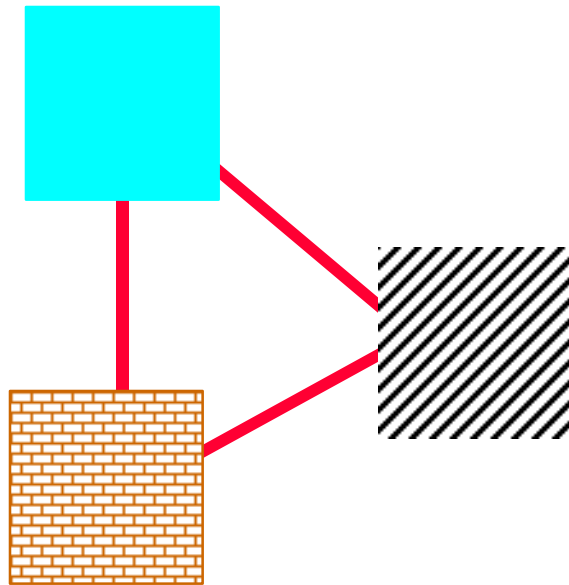
Bell Labs

gtw@research.belllabs.com

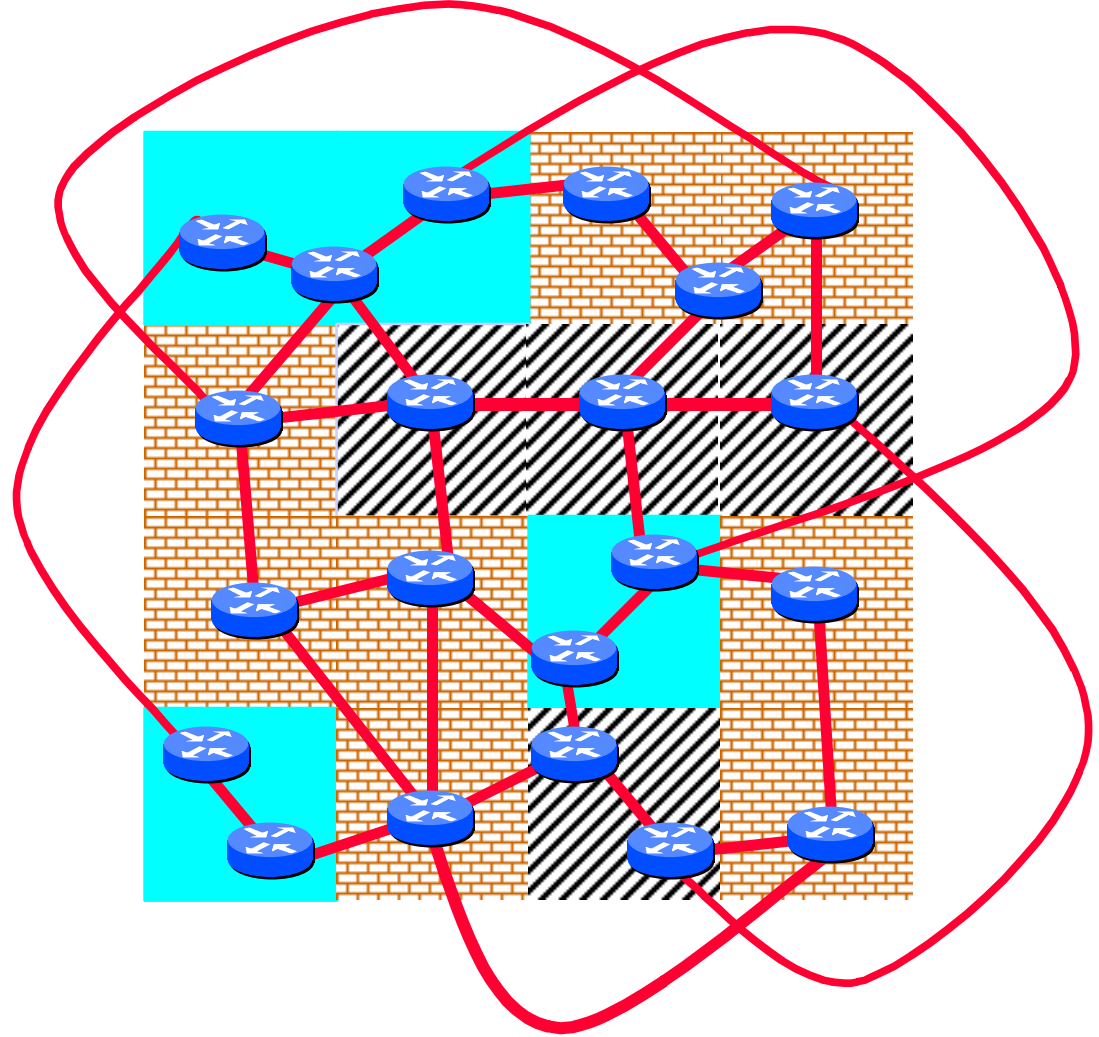
Leiden Global Internet Workshop

September, 2000

AS graphs obscure topology!



**The AS graph
may look like this.**



Reality may be closer to this...

Interior vs. Exterior Routing Protocols

Interior Gateway
Protocols (IGP) :
inside autonomous
systems

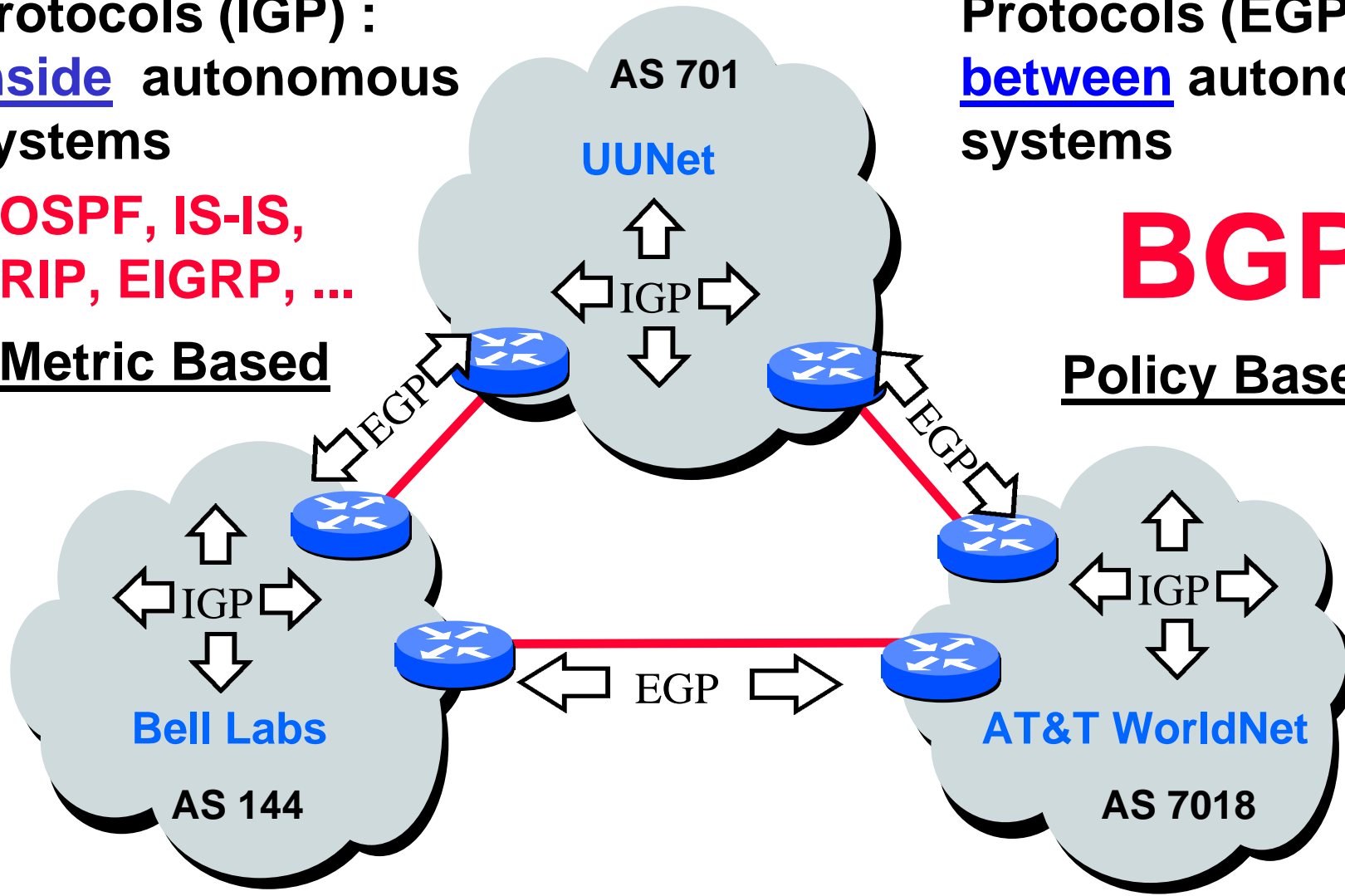
OSPF, IS-IS,
RIP, EIGRP, ...

Metric Based

Exterior Gateway
Protocols (EGP) :
between autonomous
systems

BGP

Policy Based



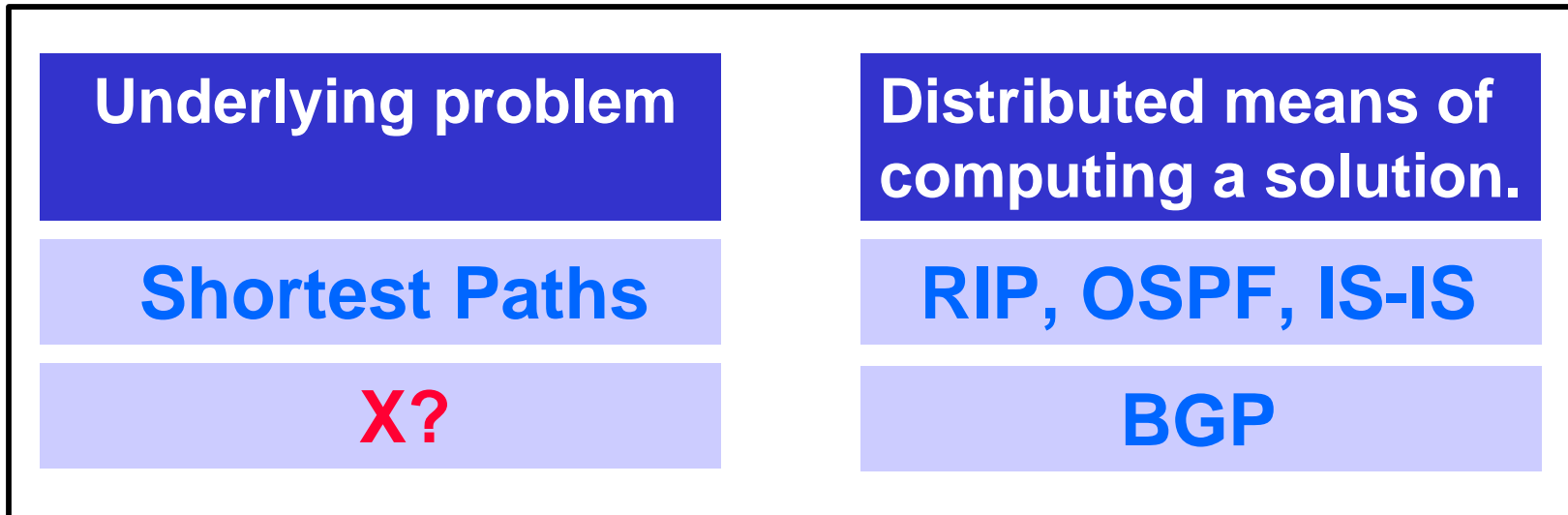
Starting point : BGP can diverge

- BGP is not guaranteed to converge to a stable routing. Policy inconsistencies can lead to “livelock” protocol oscillations.
- See “Persistent Route Oscillations in Inter-domain Routing” by K. Varadhan, R. Govindan, and D. Estrin. ISI report, 1996

Goal : A simple, tractable, and complete model of BGP routing

One application : sufficient conditions that guarantee no divergence.

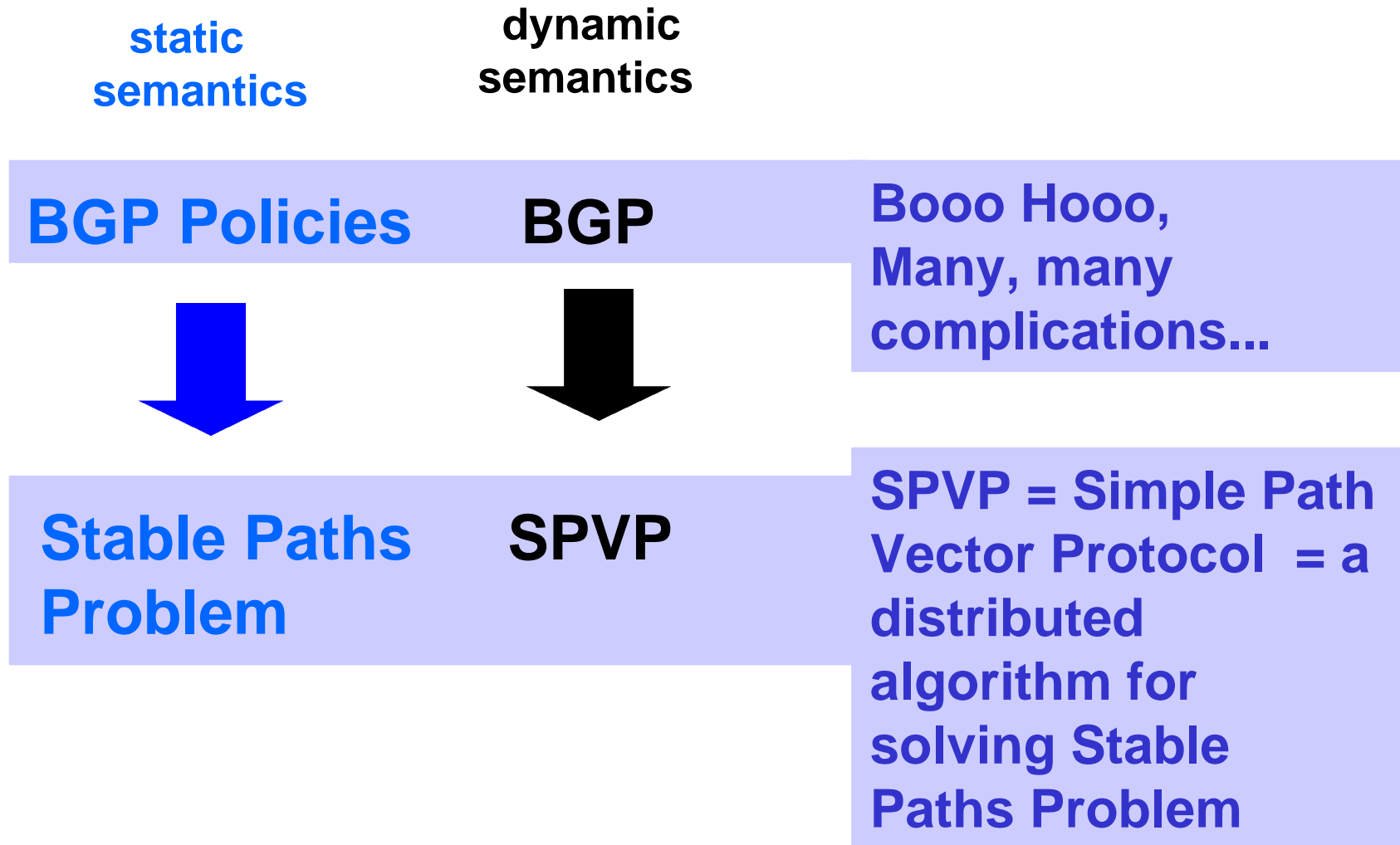
What Problem is BGP solving?



Having an **X** can

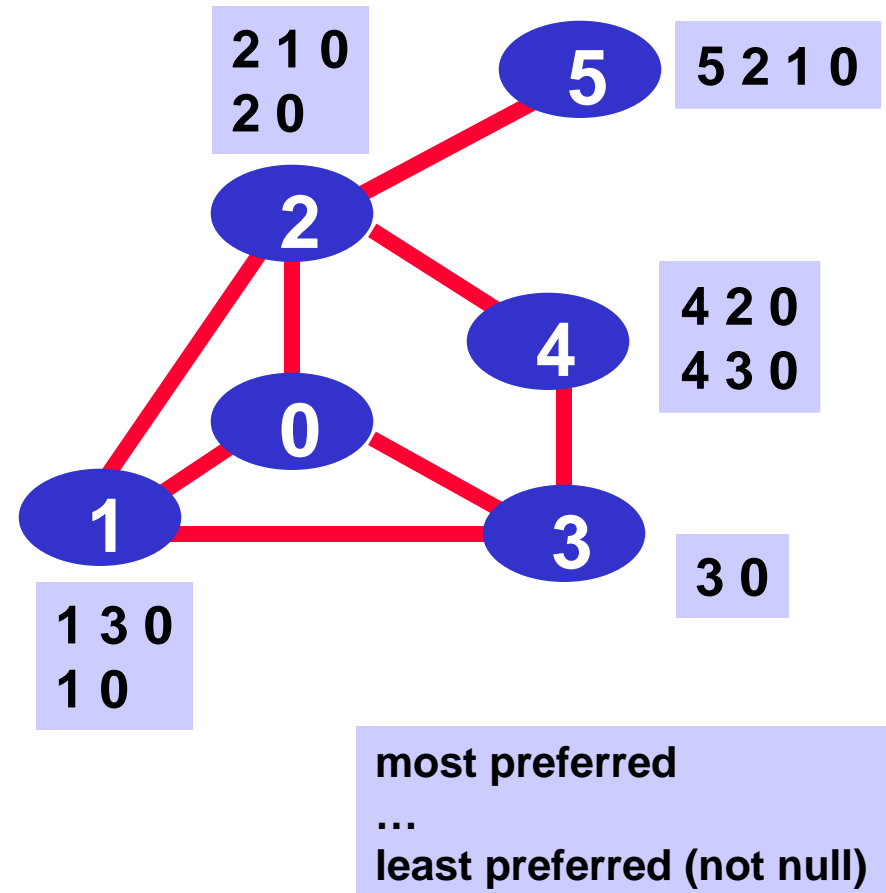
- aid in the design of policy analysis algorithms and heuristics,
- aid in the analysis and design of BGP and extensions,
- help explain some BGP routing anomalies,
- provide a fun way of thinking about the protocol

Separate dynamic and static semantics



An instance of the *Stable Paths Problem* (SPP)

- A graph of nodes and edges,
- Node 0, called *the origin*,
- For each non-zero node, a set or permitted paths to the origin. This set always contains the “null path”.
- A ranking of permitted paths at each node. Null path is always least preferred. (Not shown in diagram)



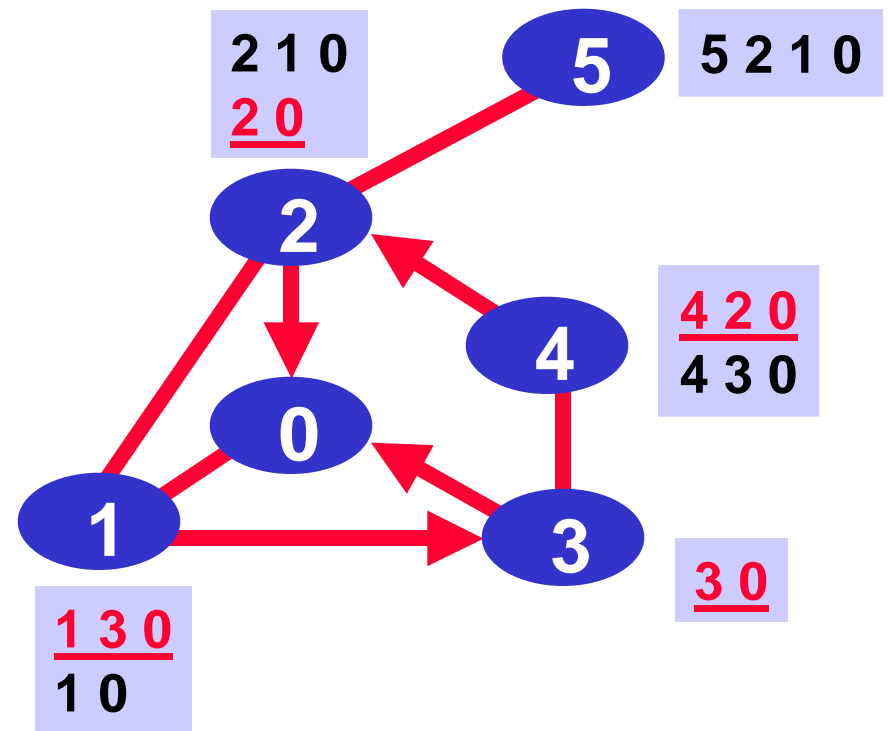
When modeling BGP : nodes represent BGP speaking routers, and 0 represents a node originating some address block

Yes, the translation gets messy!

A Solution to a Stable Paths Problem

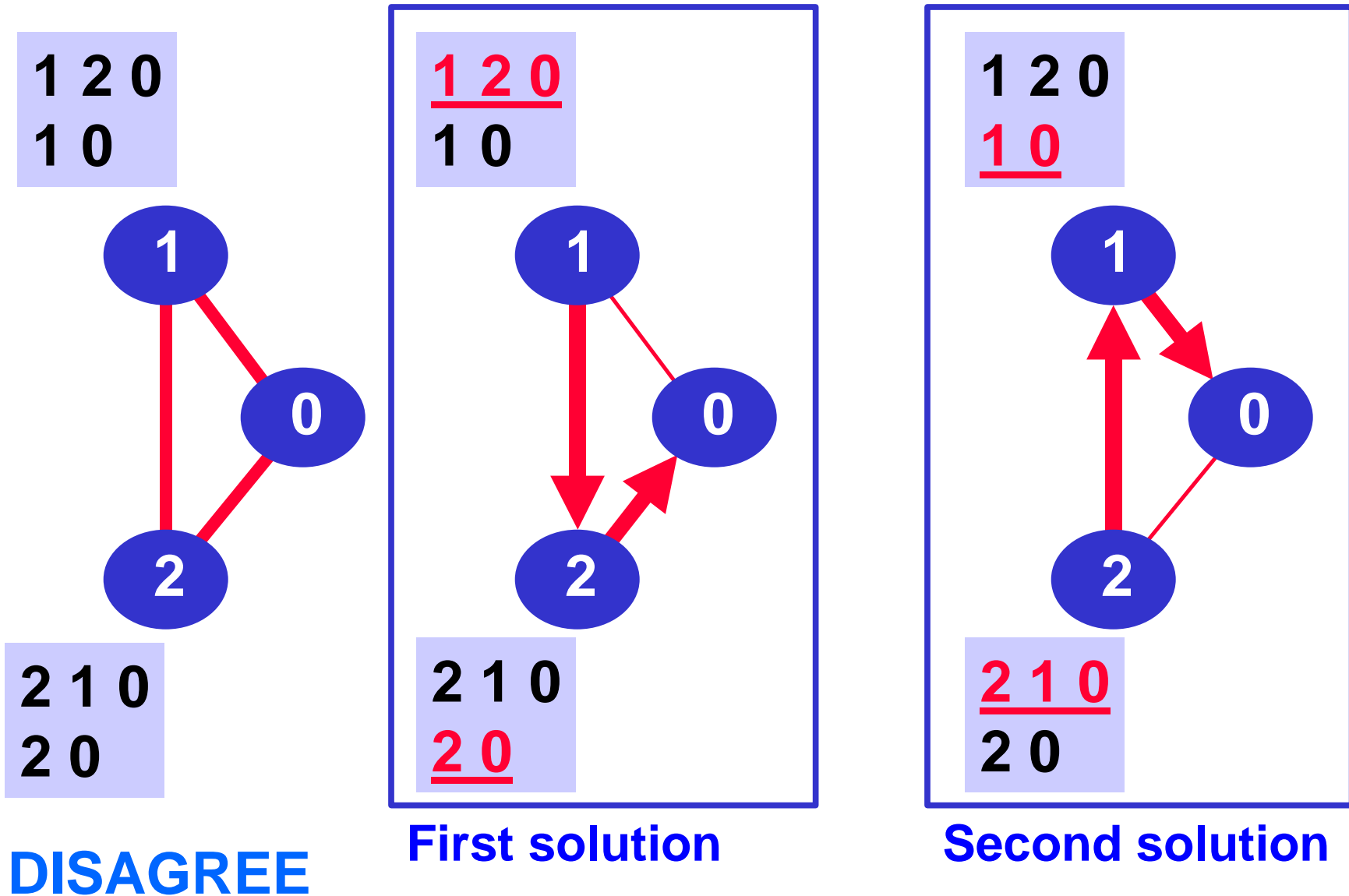
A solution is an assignment of permitted paths to each node such that

- node u 's assigned path is either the null path or is a path uwP , where wP is assigned to node w and $\{u,w\}$ is an edge in the graph,
- each node is assigned the highest ranked path among those consistent with the paths assigned to its neighbors.

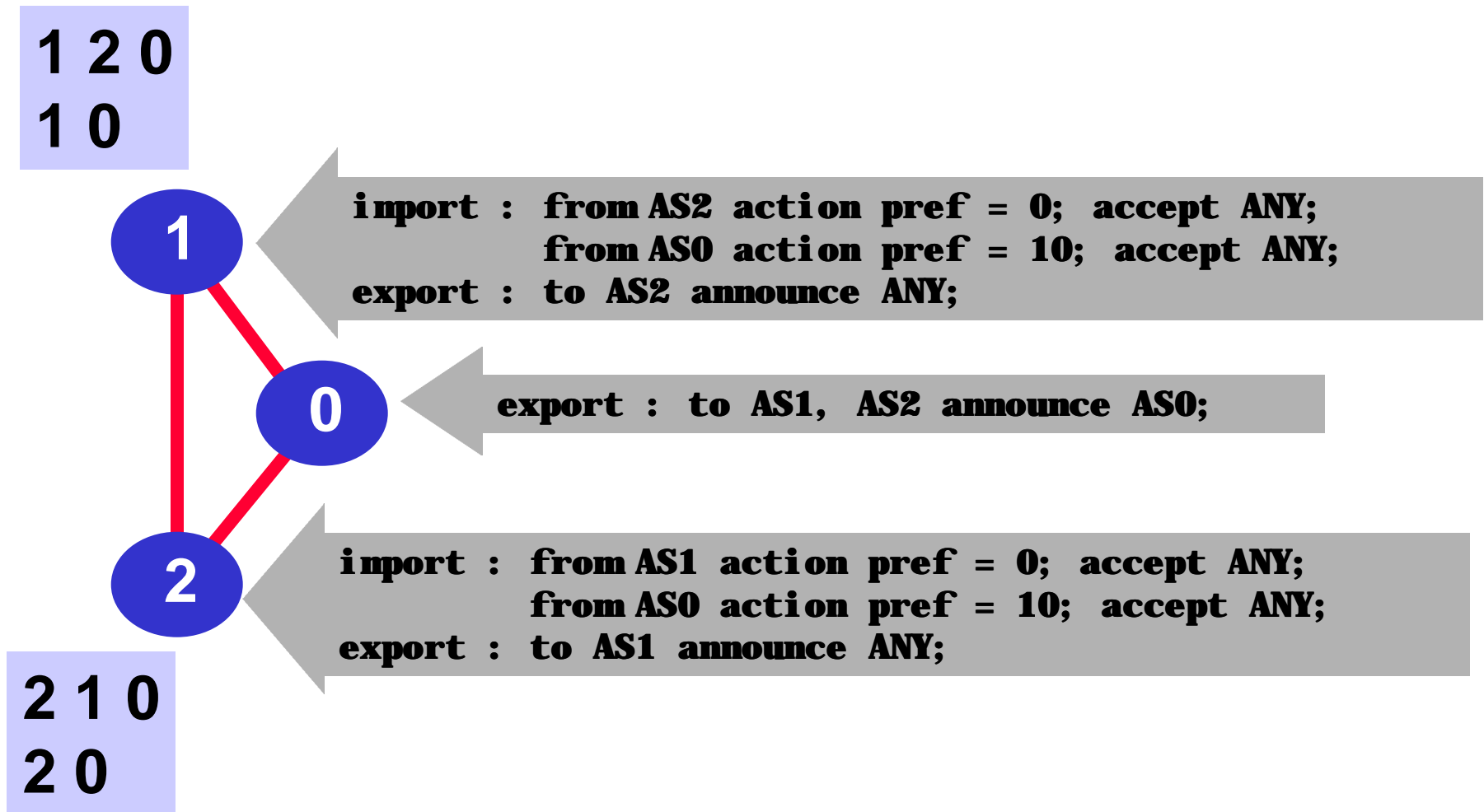


A Solution need not represent a shortest path tree, or a spanning tree.

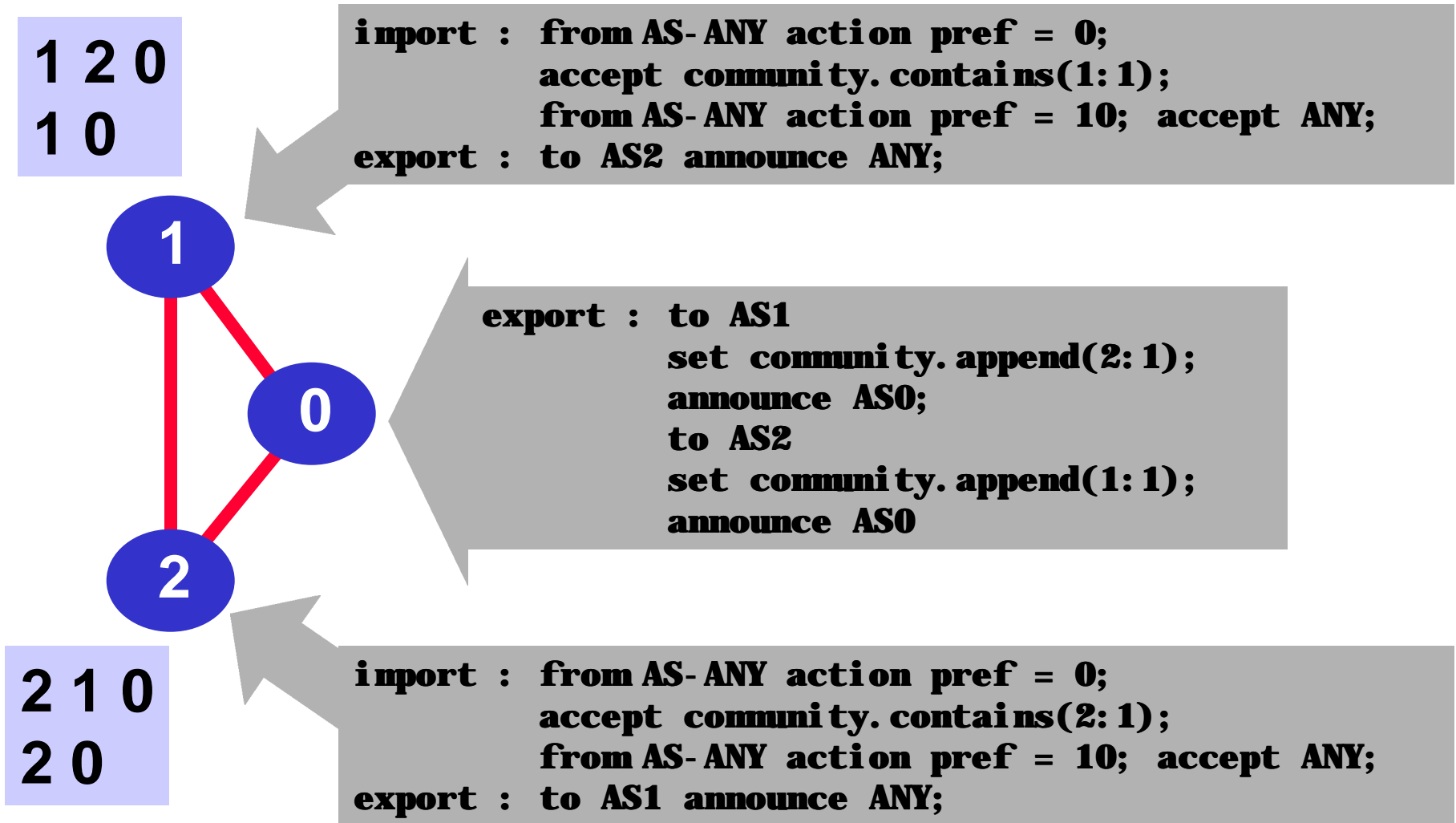
An SPP may have multiple solutions



Mapping BGP routing policies down to a Stable Paths Problem : DISAGREE in RPSL (Version I)

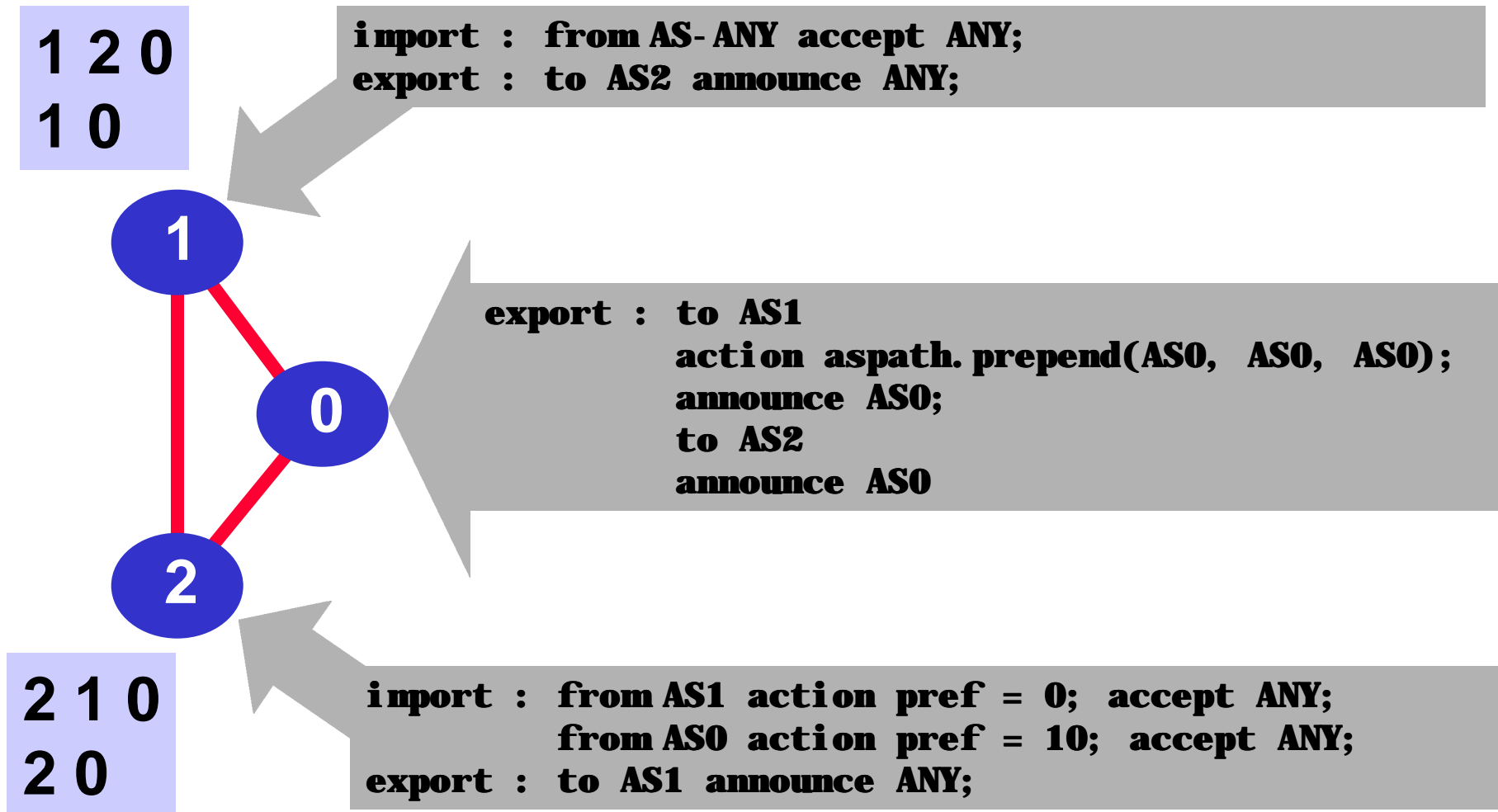


DISAGREE in RPSL (Version II)



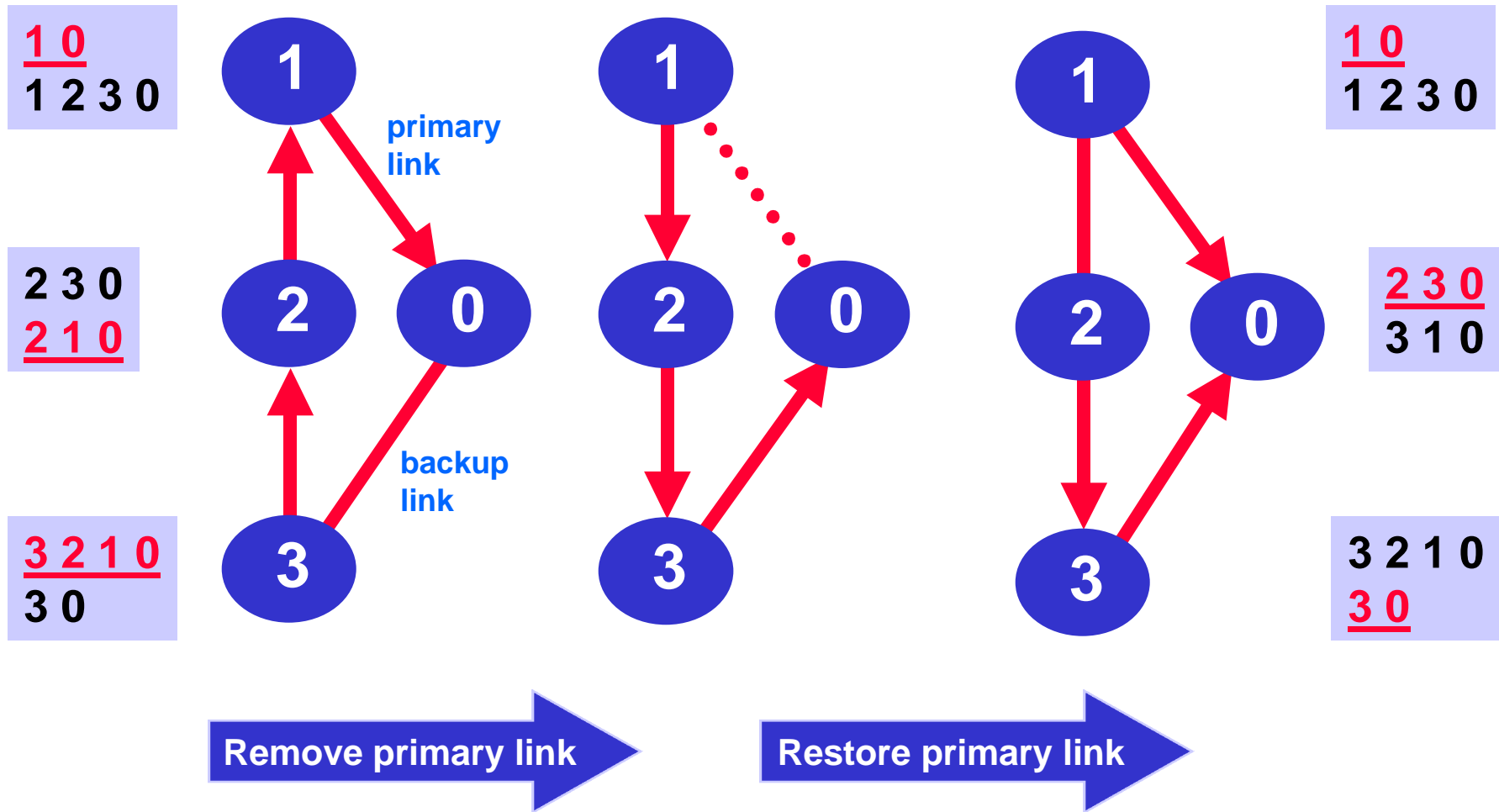
Assume AS1 and AS2 use “neighbor send-community” command

DISAGREE in RPSL (Version III)



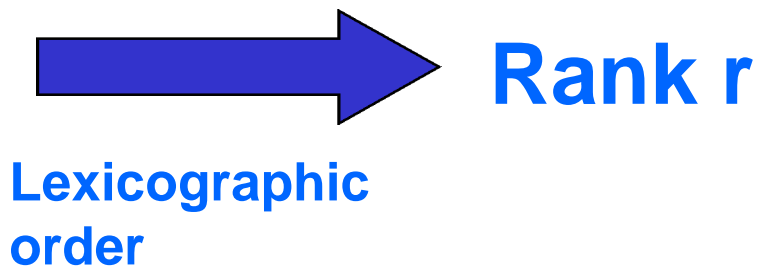
The interaction of all BGP policies is directly represented in SPP

Multiple solutions can result in "Route Triggering"



Ranking paths

$(l_p, 1/(p_l+1), \text{origin}, 1/(\text{med}+1), \text{type}, 1/(\text{igp}+1), \text{nh})$



l_p = local preference

p_l = as-path length

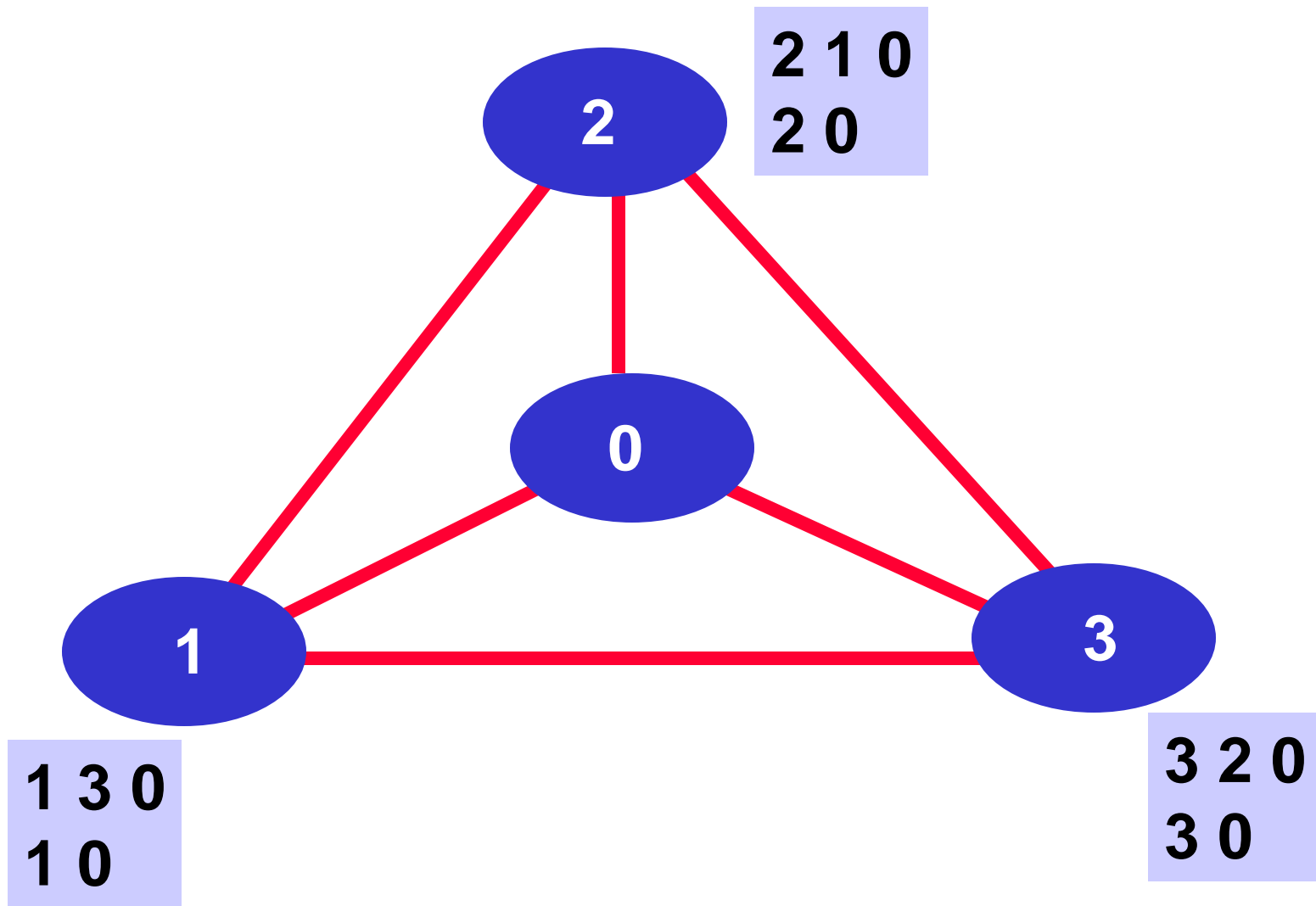
origin in {IGP, EGP, INCOMPLETE}, IGP < EGP < INCOMPLETE

type in {IBGP, EBGP}, IBGP < EBGP

igp = interior routing metric

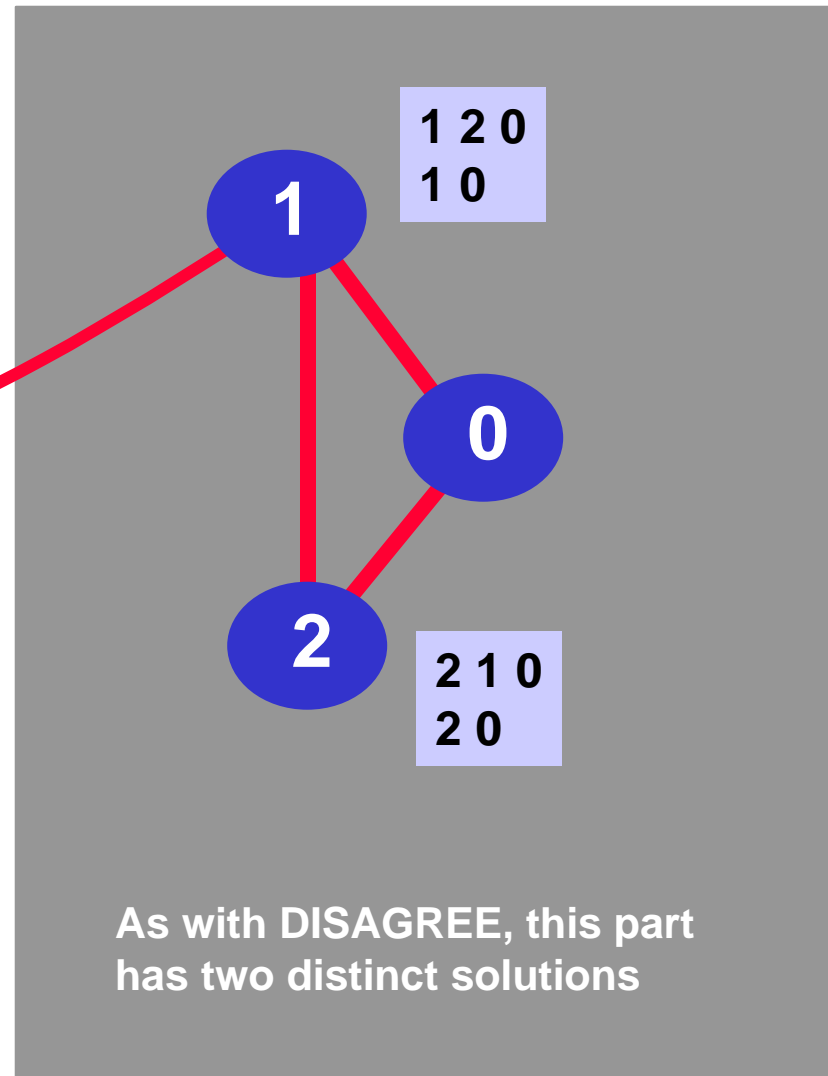
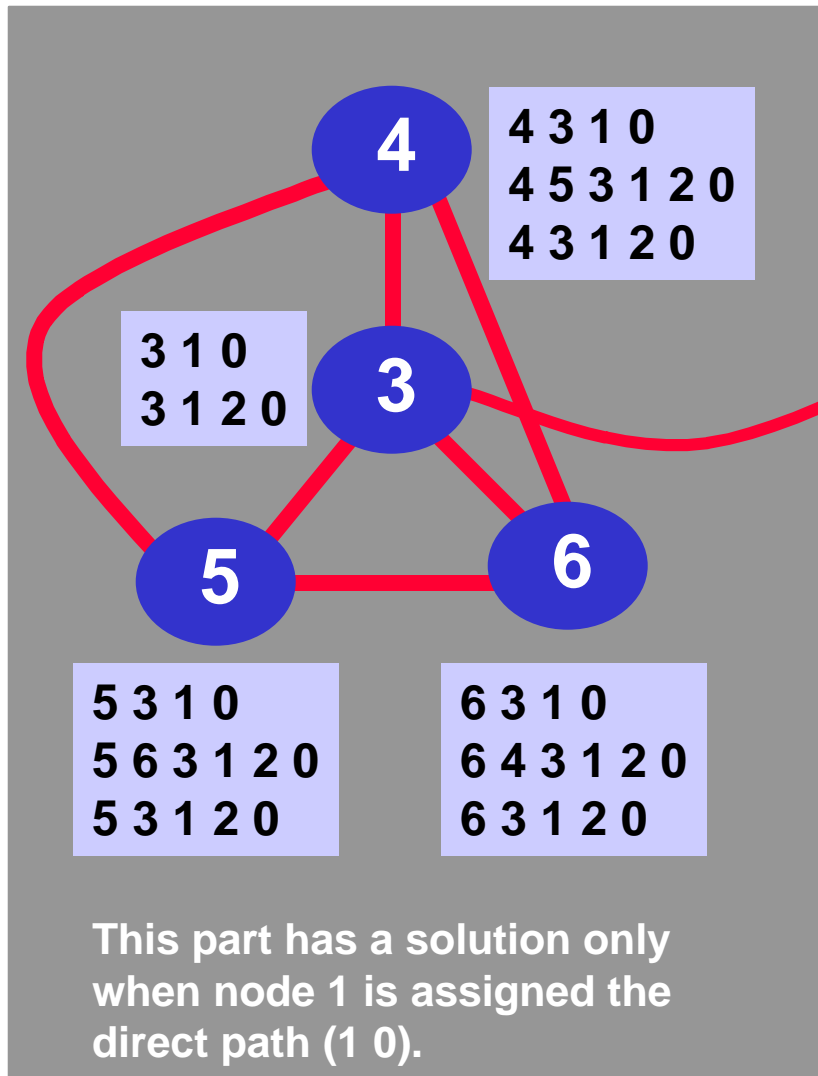
nh = next hop ip address

BAD GADGET : No Solution



PRECARIOUS

Has a solution, but can get “trapped”



Solving an SPP

**Just enumerate all path assignments
And check stability of each....**

!! Exponential complexity !!

**But, in worst case you (probably)
can't do any better...**

Remember 3-SAT?

Variables $V = \{X_1, X_2, \dots, X_n\}$

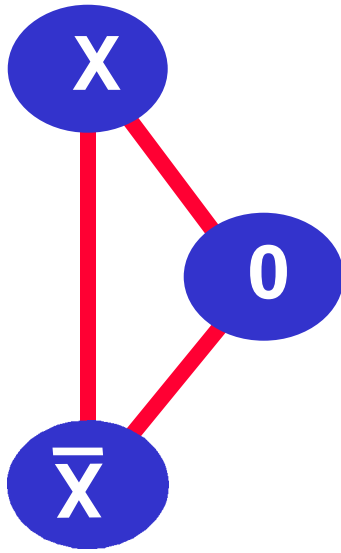
Clauses $C_1 = X_{17} \text{ or } \sim X_{23} \text{ or } \sim X_3,$
 $C_2 = \sim X_2 \text{ or } X_3 \text{ or } \sim X_{12}$
....
 $C_m = X_6 \text{ or } \sim X_7 \text{ or } X_{18}$

Question Is there an variable assignment
 $A : V \rightarrow \{\text{true}, \text{false}\}$ such that
each clause C_1, \dots, C_m is true?

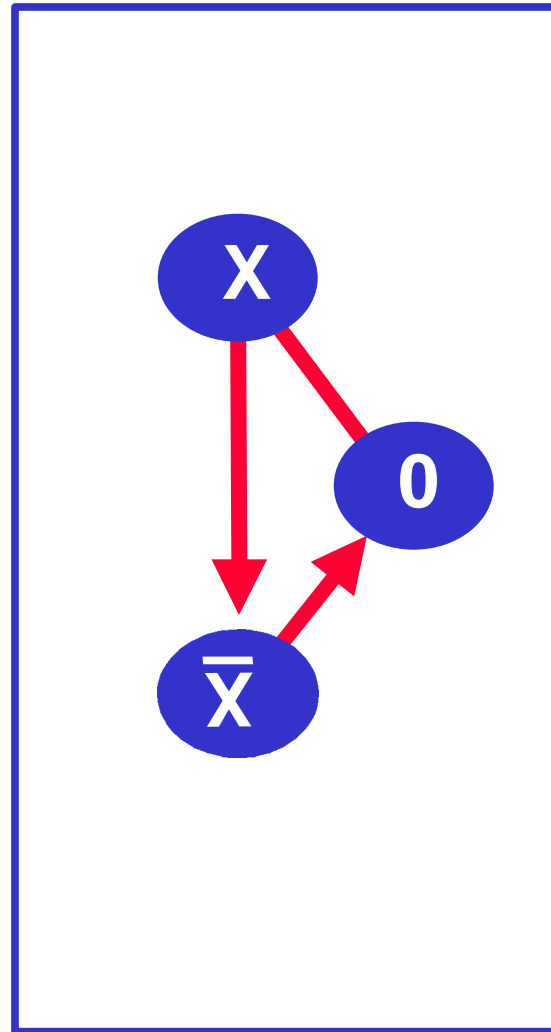
3-SAT is NP-complete

Modeling assignment to variable X

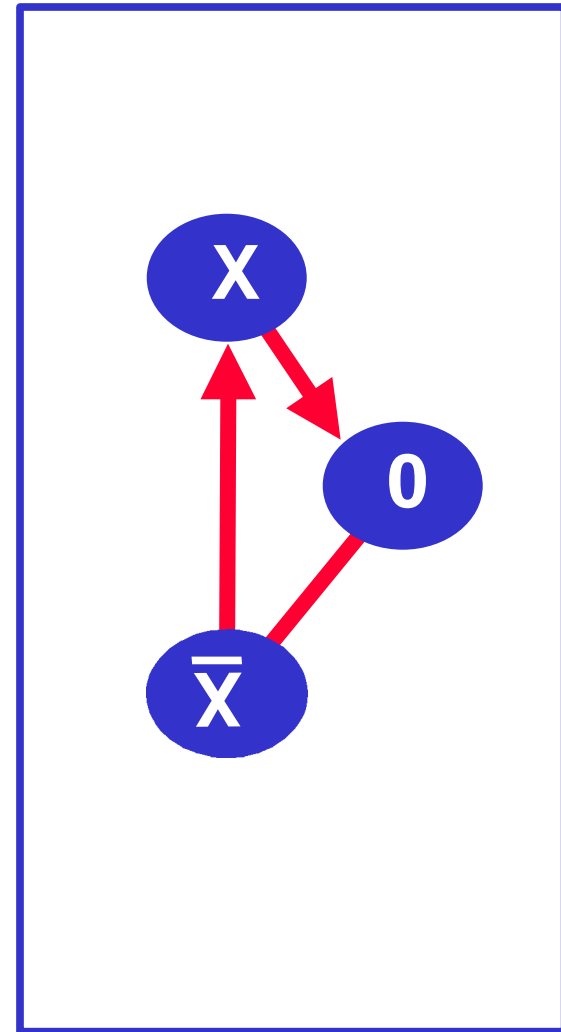
$X \bar{X} 0$
 $X 0$



$\bar{X} X 0$
 $\bar{X} 0$

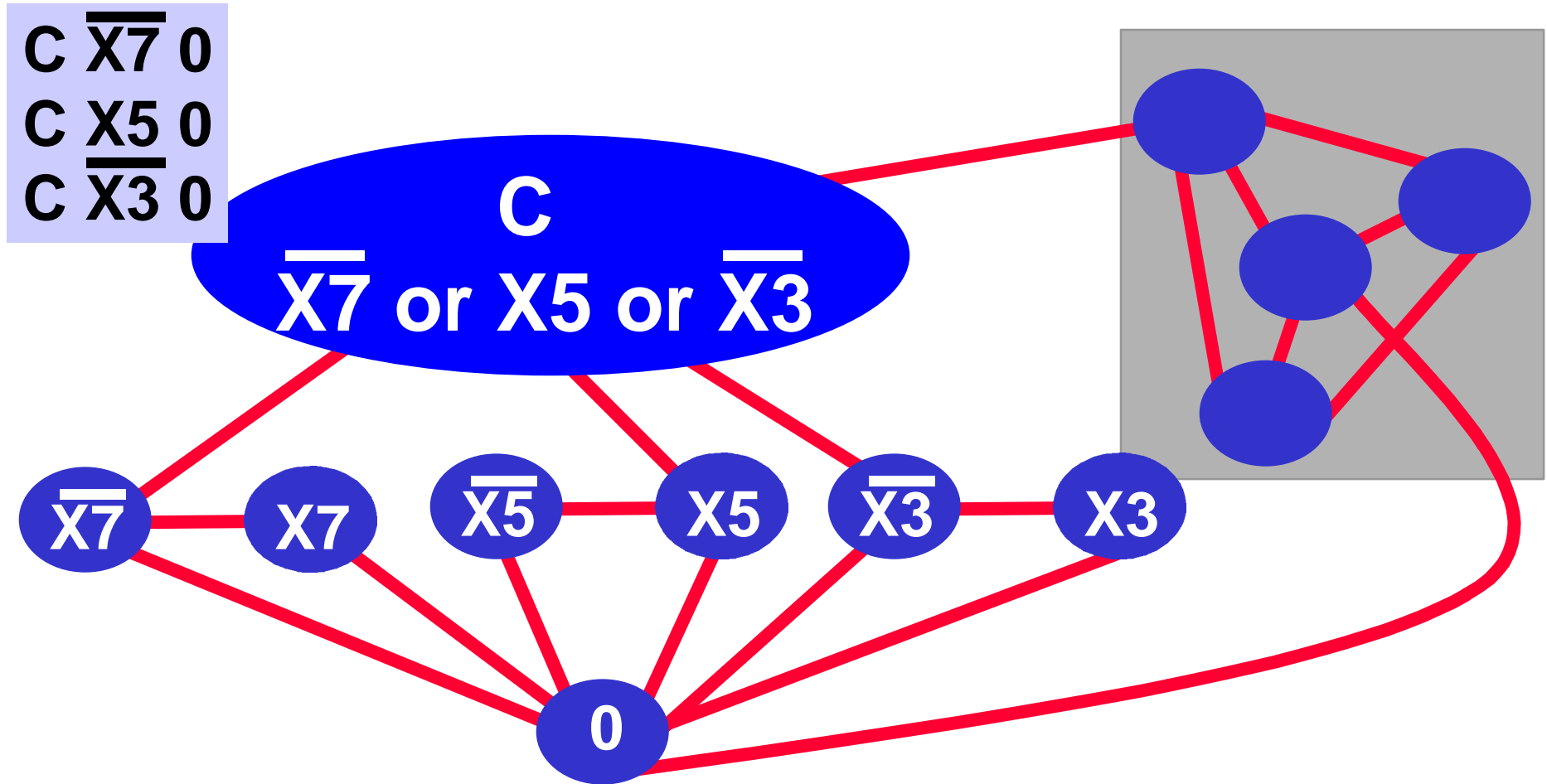


$X = \text{false}$



$X = \text{true}$

Solvability is NP-complete



Distributed algorithms to solve SPP?

- **OSPF-like :**
 - Distribute topology, path ranks
 - Solve SPP locally
 - **Exponential worst case**
 - **How can loops be avoided when multiple solutions exist?**
- **RIP-like:**
 - Pick the best path from the set of your neighbor's paths, tell your neighbors when you change your mind
 - **Can diverge**
 - **Not guaranteed to find a solution, even when one exists**
 - **No bound on convergence time**

SPVP protocol

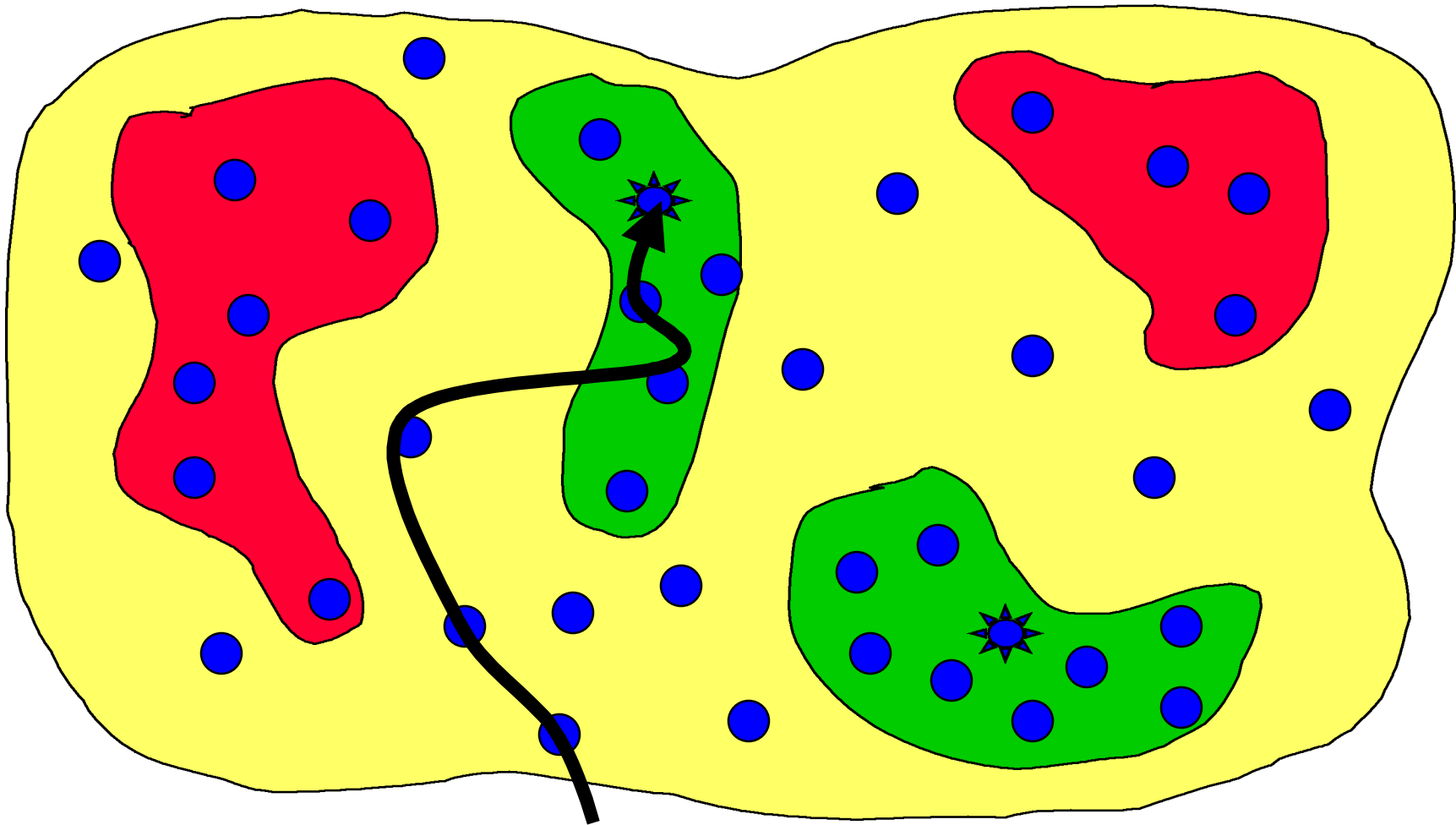
Pick the best path available at any given time...

```
process spvp[u]
{
  receive P from w →
  { rib-in(u←w) := u P
    if rib(u) != best(u) {
      rib(u) := best(u)
      foreach v in peers(u) {
        send rib(u) to v
      }
    }
  }
}
```

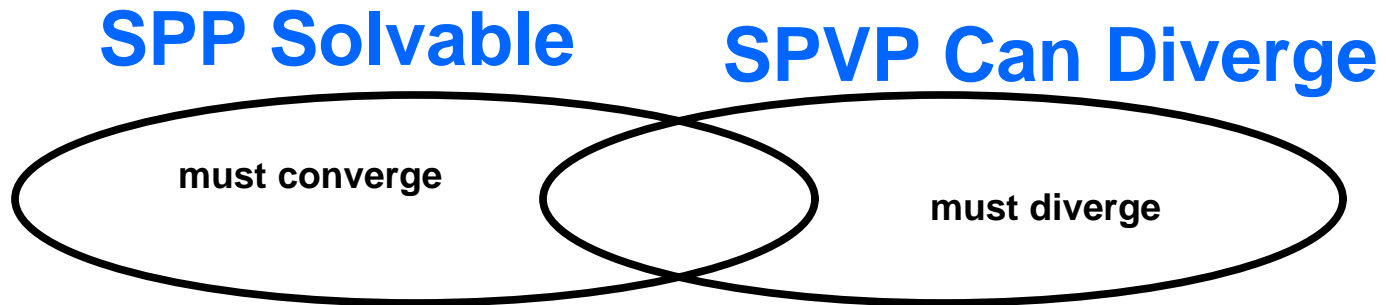
SPVP wanders around assignment space

● = assignment

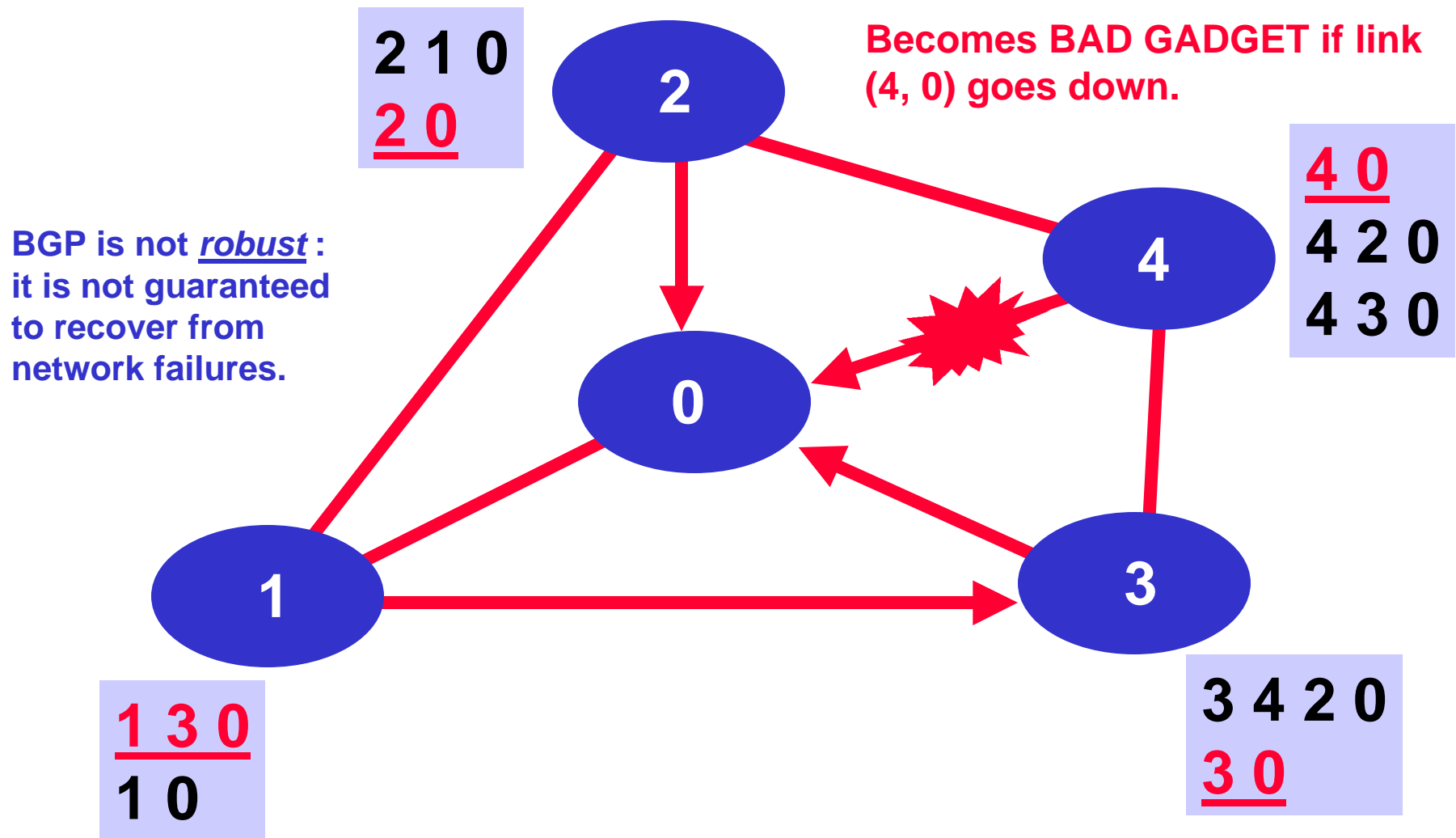
★ = solution



Another Picture

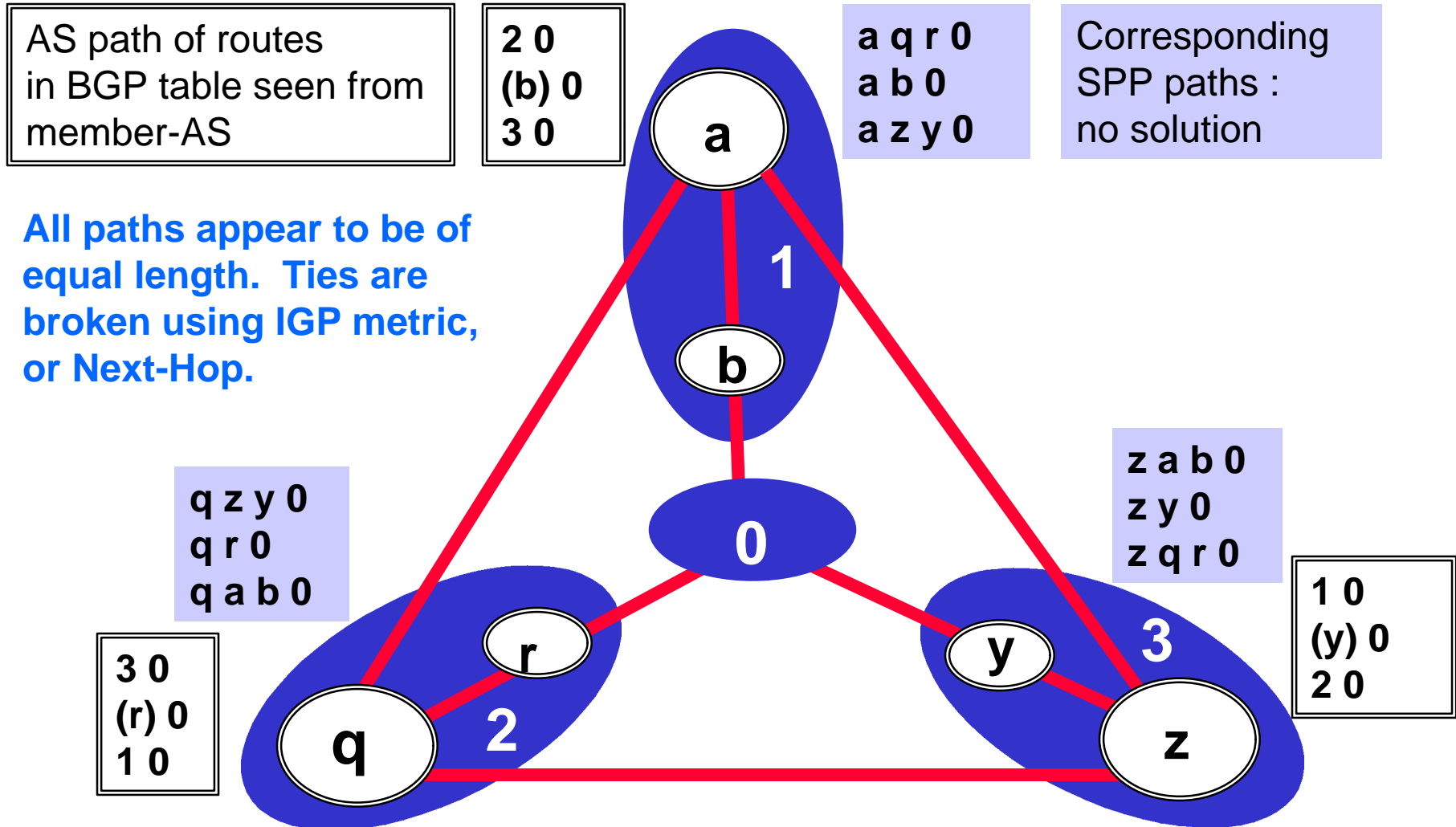


SURPRISE : Beware of Backup Policies

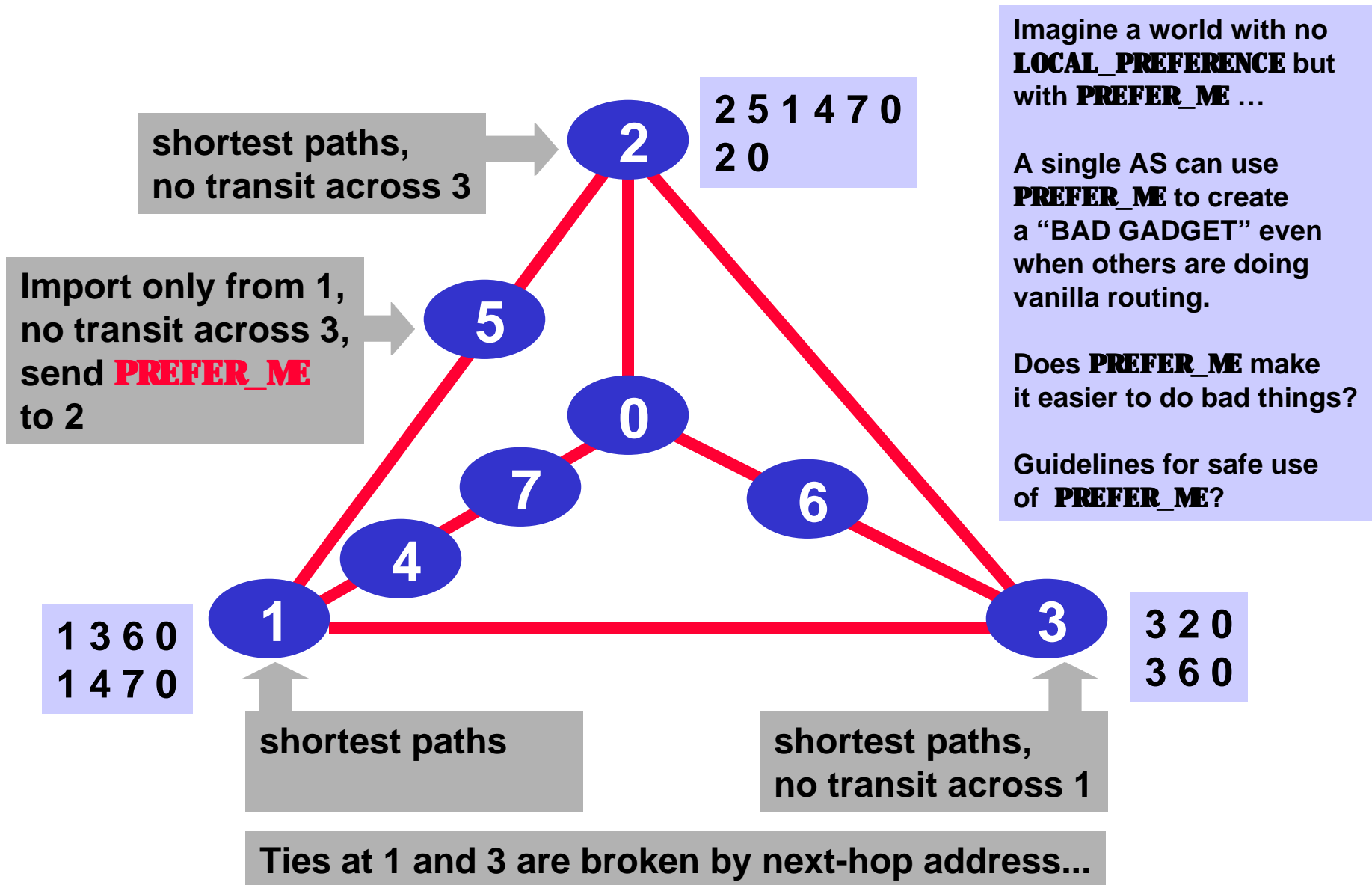


SPP simplifies analysis of proposed extensions

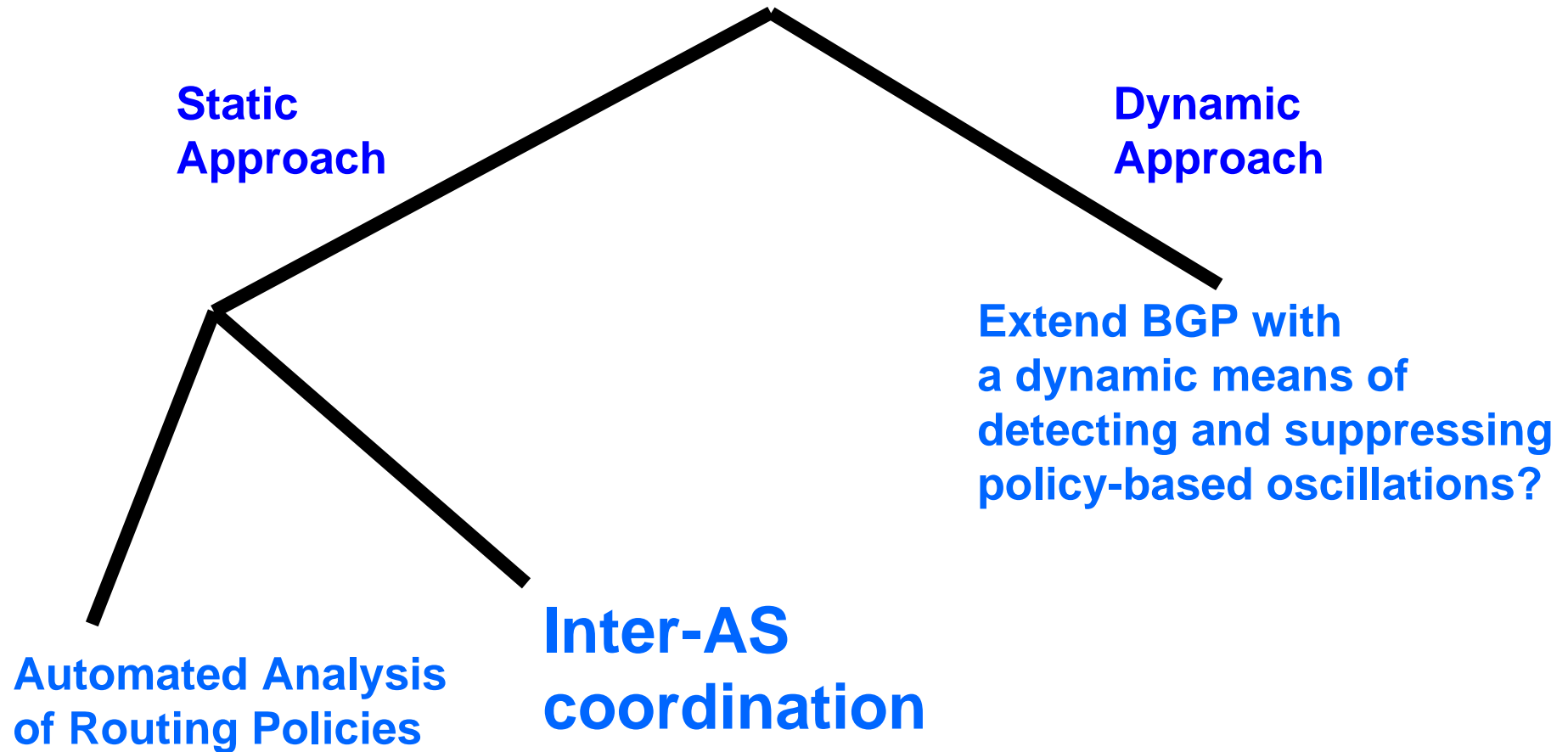
Proposal : Allow AS-path length to include member ASes within a confederation.



PREFER_ME Global Community?



What is to be done?



These approaches are complementary

A sufficient condition for sanity

If an instance of SPP has an acyclic dispute digraph, then

Static (SPP)

solvable

unique solution

**all sub-problems
uniquely solvable**

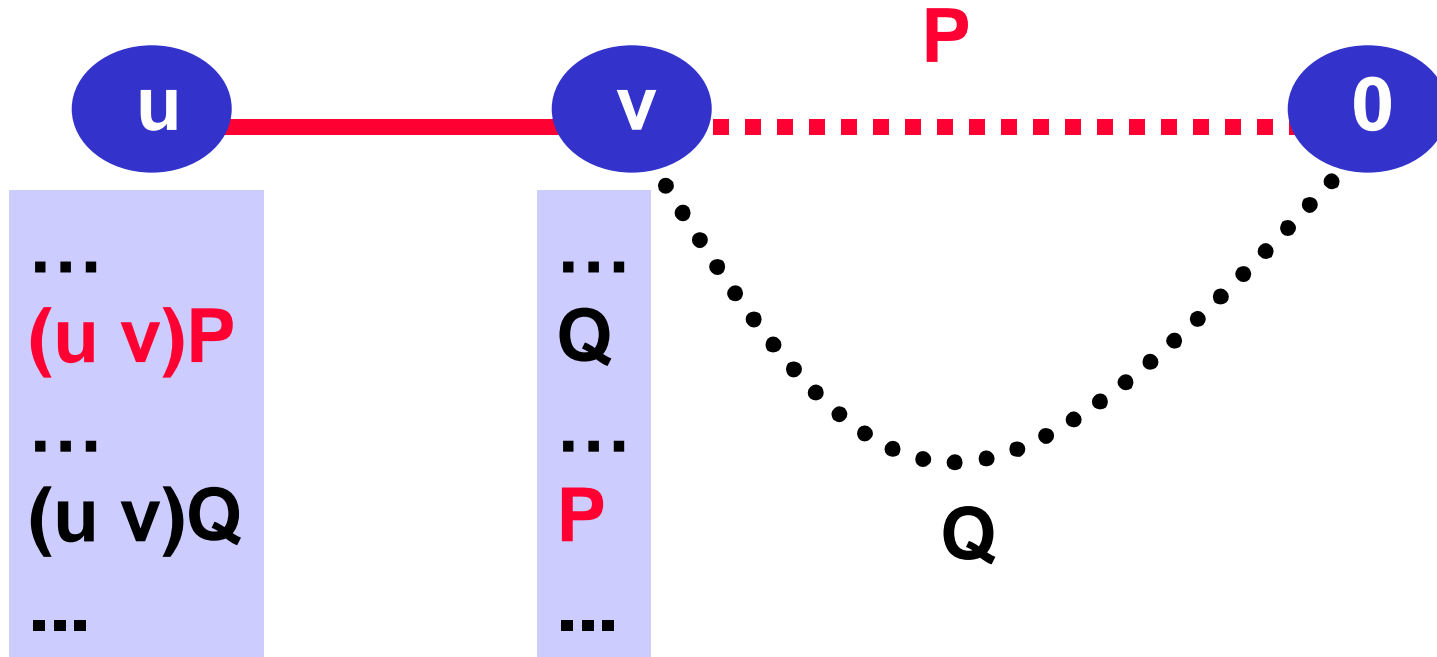
Dynamic (SPVP)

safe (can't diverge)

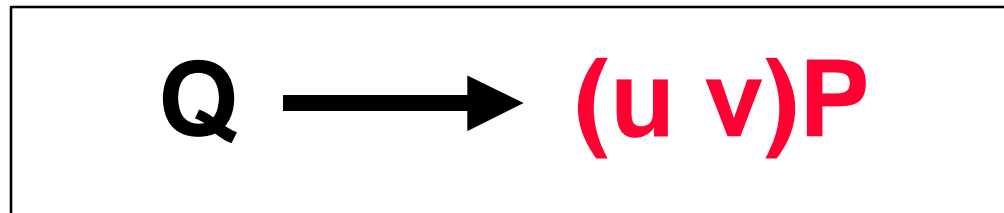
predictable restoration

**robust with respect to
link/node failures**

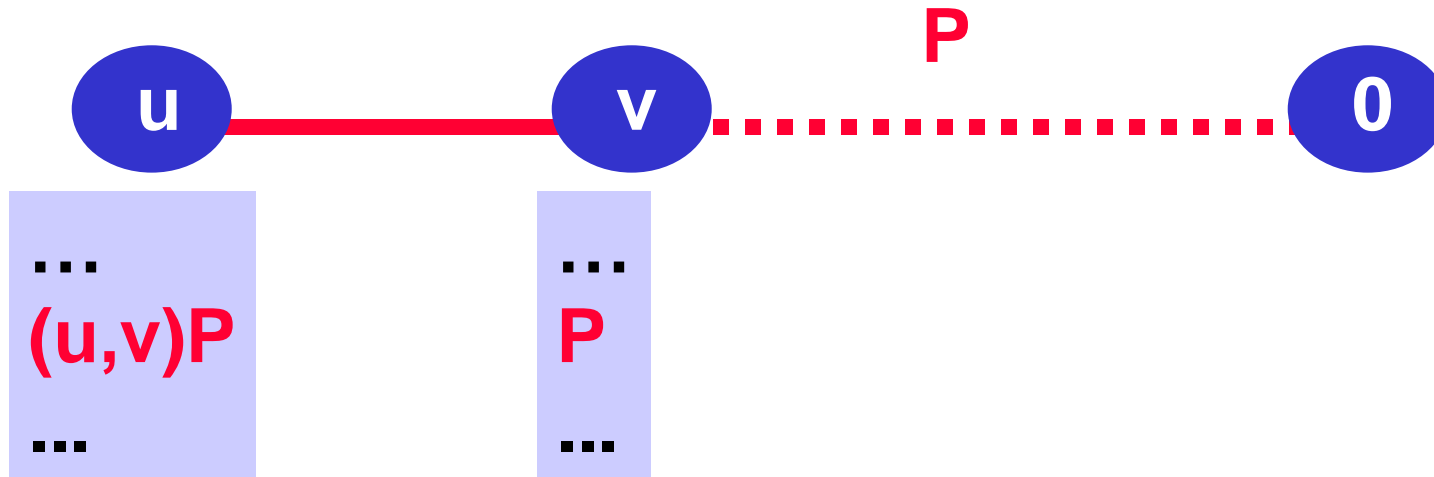
Dispute Digraph



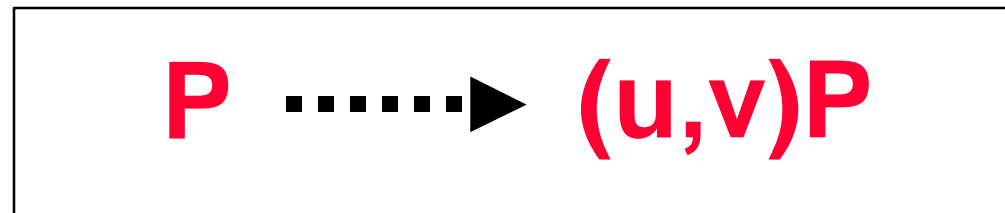
Gives the *dispute arc*



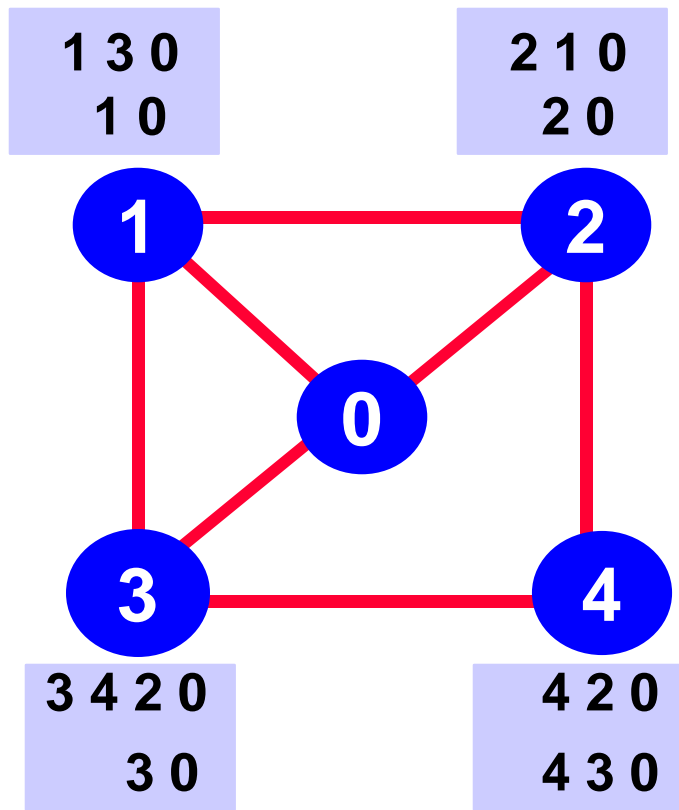
Dispute Digraph (cont.)



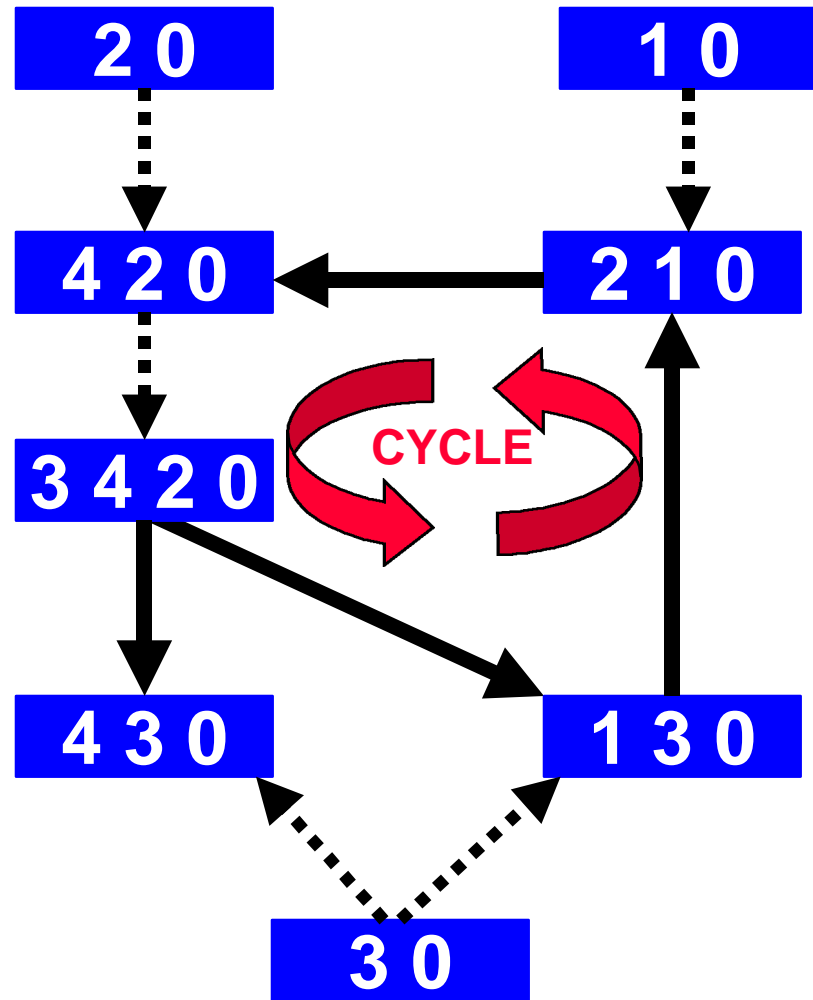
Gives the *transmission arc*



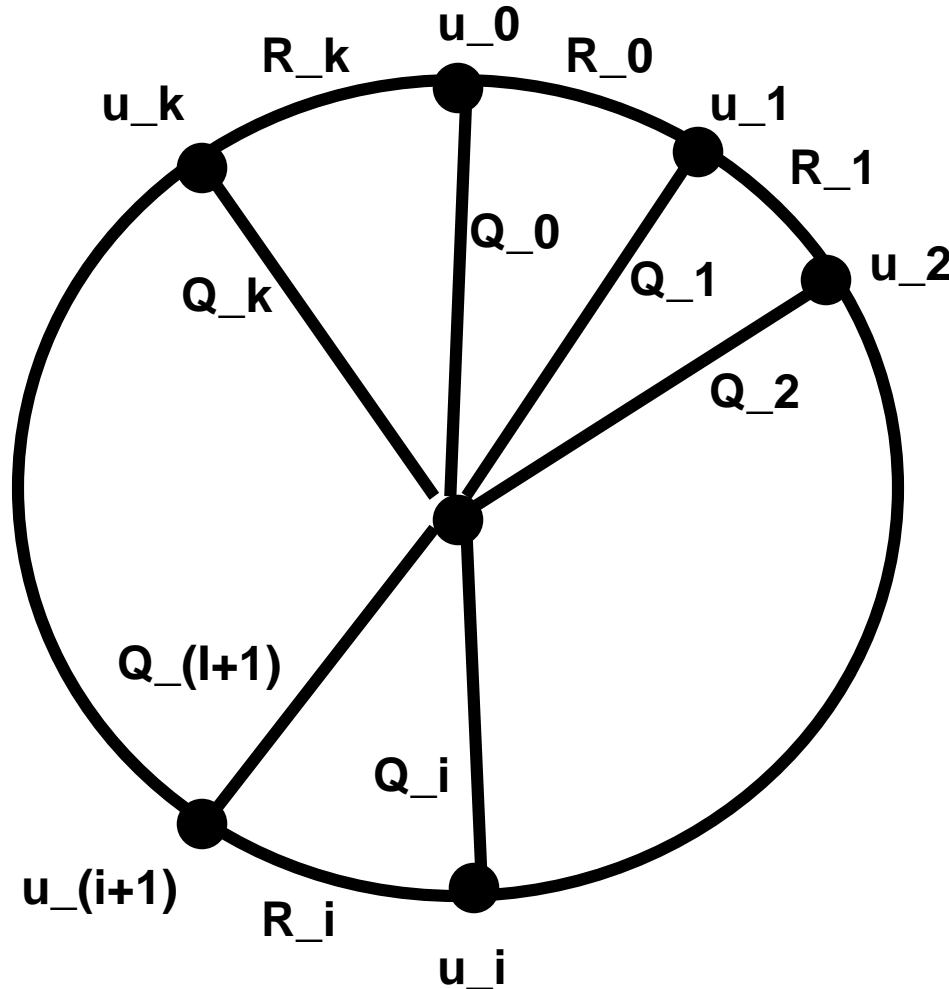
Dispute Digraph Example



BAD GADGET II



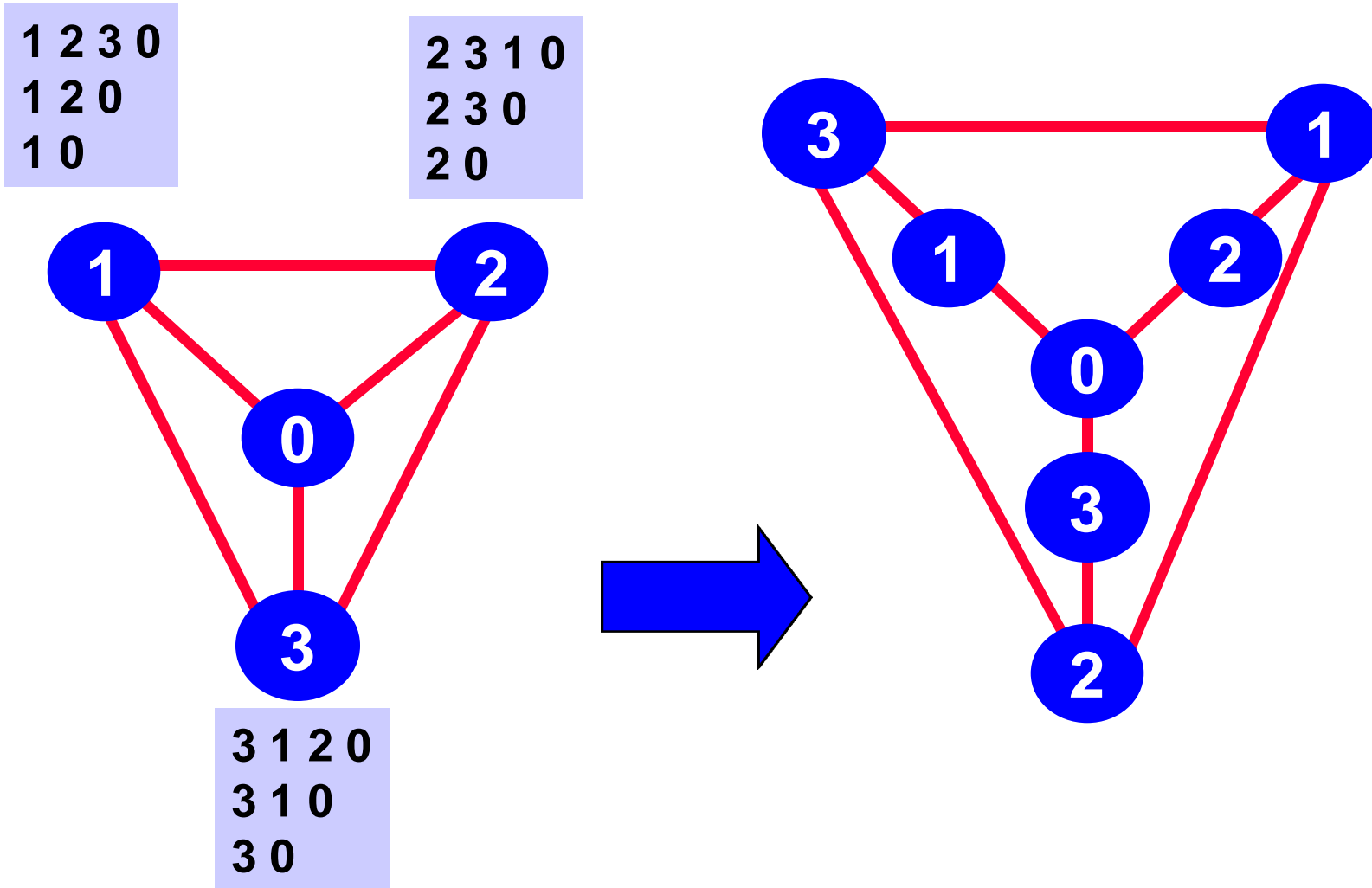
Dispute Wheels



At u_i , rank of Q_i is less than or equal to rank of $R_i Q_{(i+1)}$

There exists a dispute wheel iff there exists cycle in the dispute digraph

Dispute Wheel Example

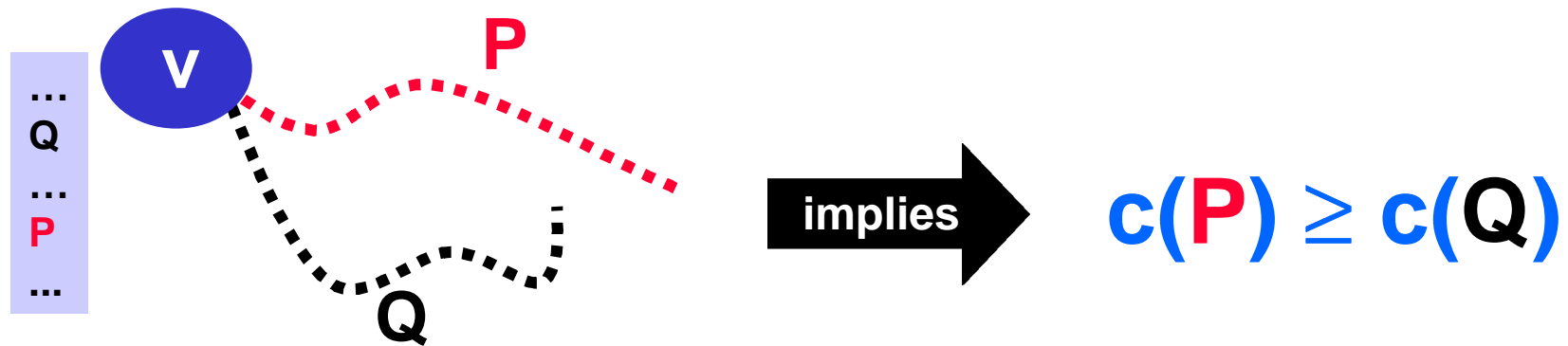


An Application

c is a cost function on edges.

c is *coherent* if all cycles have positive cost.

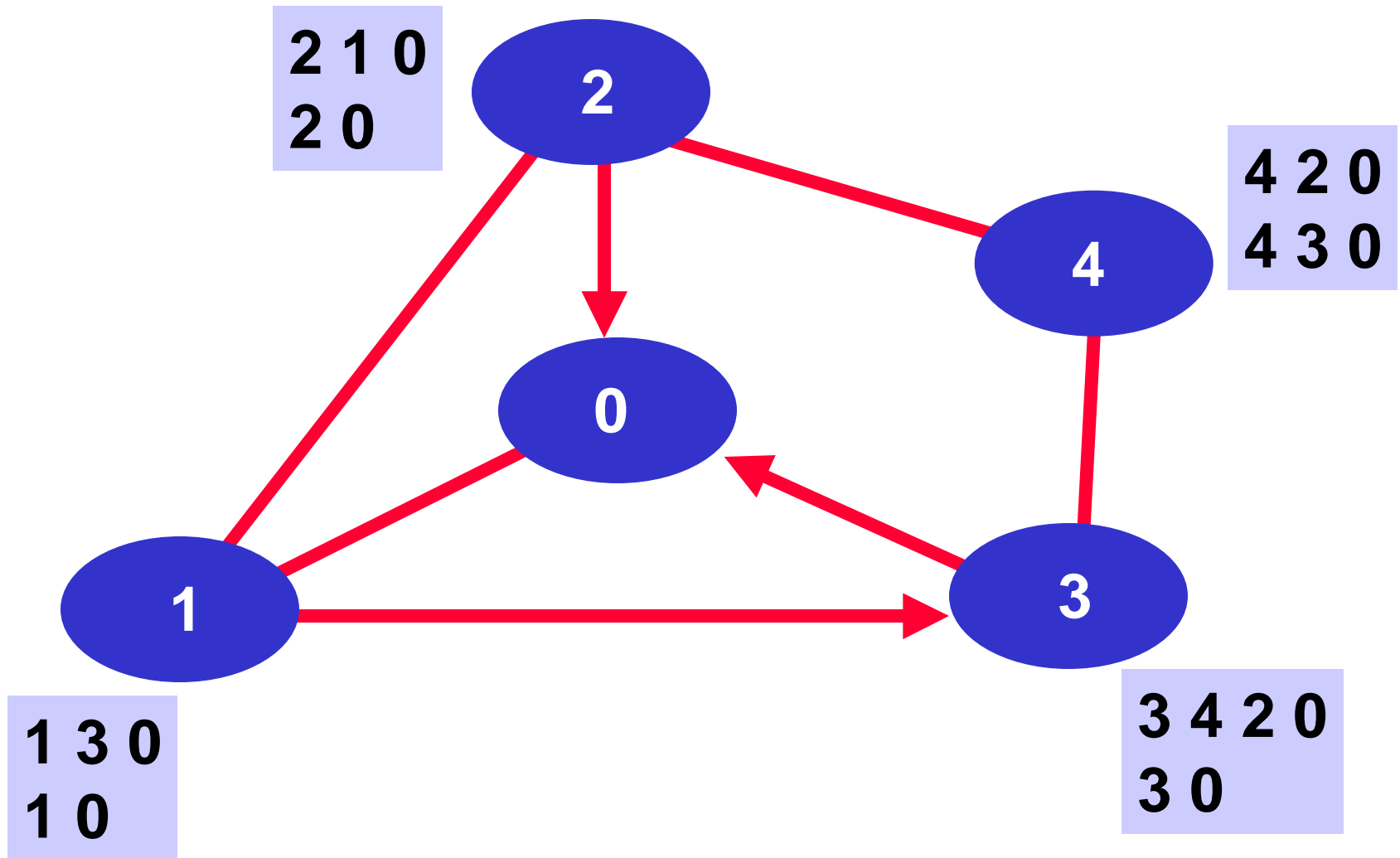
An SPVP specification is *consistent with c* if



A Dynamic Solution

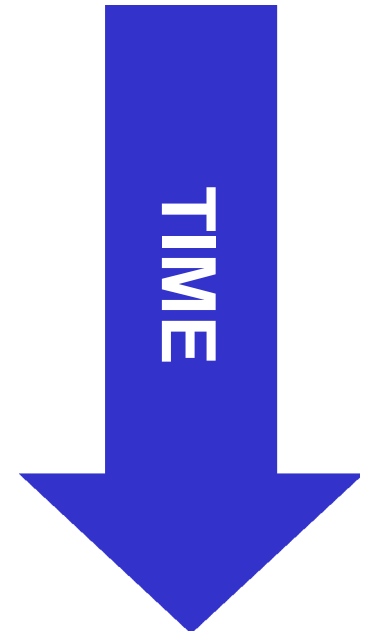
- Extend SPVP with a **history** attribute,
- A route's history contains a path in the dispute digraph that “explains” how the route was obtained,
- A route history will contain a dispute cycle **if and only if** a policy dispute is dynamically realized.
- If a route's history contains a cycle, then suppress it

BAD GADGET II



A History Trace for Bad Gadget II

path	event history for path
1 : (1 0)	e
2 : (2 0)	e
3 : (3 4 2 0)	e
4 : (4 2 0)	e
...	...
1 : (1 0)	e
2 : (2 1 0)	(+ 2 1 0)
3 : (3 0)	(- 3 4 2 0) (- 4 2 0) (+ 2 1 0)
4 : ()	(- 4 2 0) (+ 2 1 0)
...	...
1 : (1 3 0)	(+ 1 3 0) (- 3 4 2 0) (- 4 2 0) (+ 2 1 0)
2 : (2 1 0)	(+ 2 1 0)
3 : (3 0)	(- 3 4 2 0) (- 4 2 0) (+ 2 1 0)
4 : ()	(- 4 2 0) (+ 2 1 0)
...	...
1 : (1 3 0)	(+ 1 3 0) (- 3 4 2 0) (- 4 2 0) (+ 2 1 0)
2 : (2 0)	(- 2 1 0) (+ 1 3 0) (- 3 4 2 0) (- 4 2 0) (+ 2 1 0)
3 : (3 0)	(- 3 4 2 0) (- 4 2 0) (+ 2 1 0)
4 : ()	(- 4 2 0) (+ 2 1 0)



A CYCLE!

What's going on ?

Dynamic cycles of event history
correspond exactly to static cycles
in the dispute digraph.

To Do

- **Implementation of Histories (in SSFNET?)**
 - problems include (1) compatibility with full set of BGP features, (2) robustness, (3) scalability, (4) configuration/management interface
- **Heuristics for analysis of RPSL**
- **Analysis of “backup routing”**

Work in Progress...

“An Analysis of BGP Convergence Properties”

Timothy G. Griffin, Gordon Wilfong

SIGCOMM'99

 **Model BGP, show static analysis is hard**

“Policy Disputes in Path Vector Protocols”

Timothy G. Griffin, F. Bruce Shepherd, Gordon Wilfong

ICNP '99

 **Define Stable Paths Problem and develop sufficient condition for “sanity”**

“A Safe Path Vector Protocol”

Timothy G. Griffin, Gordon Wilfong

INFOCOM'00

 **Dynamic solution based on histories**

“Stable Internet Routing without Global Coordination”

Lixin Gao, Jennifer Rexford

SIGMETRICS'00

 **Show that if certain guidelines are followed, then all is well.**

Links

www.research.att.com/~griffin

www.research.att.com/~griffin/interdomain.html